



Calhoun: The NPS Institutional Archive

DSpace Repository

Theses and Dissertations

1. Thesis and Dissertation Collection, all items

1955

Similitude considerations in neutron and gamma ray scattering.

Ney, Kenneth C.

Iowa State College

http://hdl.handle.net/10945/14581

Downloaded from NPS Archive: Calhoun



Calhoun is the Naval Postgraduate School's public access digital repository for research materials and institutional publications created by the NPS community. Calhoun is named for Professor of Mathematics Guy K. Calhoun, NPS's first appointed -- and published -- scholarly author.

> Dudley Knox Library / Naval Postgraduate School 411 Dyer Road / 1 University Circle Monterey, California USA 93943

http://www.nps.edu/library

SIMILITUDE CONSIDERATIONS IN NEUTRON AND GAMMA RAY SCATTERING

Kenneth C. Ney

Library
U. S. Naval Postgraduate School
Monterey, California













SILLIAN COLLA COL SCALLING

25

Kenneth C. Ney

A Thesis Submitted to the
Craduate Faculty in Partial Fulfillment of
The Requirem ats for the Degree of
MASI A O. SCHAGE

Major Subject: Nuclear Ingineering

TALL C' CCLLIES

		Tago
	INITATOM	a see
Link #	MINIM OF HER PARTIES	2
aporter sere	SCOTE OF THE PICAL OF	5 2
IV.	TIDE IICH ATIBI	5
	A. Assumptions B. Noutron Scattering C. Germa Ray Scattering	5 30 27
Att.	TOP WITTE AT THE ACT	32
	A. Exterials B. Equipment C. Procedure	32 33 37
Topogra	A PRINTING TOOLS OF A LOCALISION	43
	A. Neutron Conviering B. Germa Ray Sear toring G. Gowerel Miscoscion	13 17 50
VII.	CONCLUMICATION	52
Paripages one	Le 1 Addie Carles	53
and the	ACT MILLIAM TO THE CO.	S. S. S.
7.	APTLOTA	55
	A. Sample Applitheal Computations	55



I. I. Call

The current development of nuclear powered aircraft involves any problems which are relatively unit portant in the design of large per mently located reactors. One of these problems is the design of shielding arran events which will naturally reduce the weight of the shield and jet sufficiently rotect the crow. One possibility is the use of a shalow shield between the reactor and the crew compartment. Another is a split shield where the shielding placed next to the reactor reduces the relation to some degree and additional shielding placed around the crew compartment reduces the radiation within the compartment to permissible levels.

reactor-produced neutron and arrange, reliation will be scattered by the structure of the aircraft. To do in the smield properly, the amount of this scattered radiation that enters the crew compartment rust be found. This can wither be done by nath marical or direct measurement methods.

Considering the camplex structure that an airplane necessarily has, the latter method employing a model on the airplane is probably the more found that any.

Thus, the relationship content the scattering by the rodel and the full-scale structure must be known. This relationship with a simplified structure was the object of this investigation.

the statement of the st _____ • All the same of th A STATE OF THE PARTY OF THE PAR

II. REVILLE OF HER CATUME

No investigations on the subject of similitude considerations in the scatt ring of neutrons and paras rays by structural material were found in the literature. However, many studies related to this subject are available.

Chasgow (1) investigated the scattering of neutrons from the walls and air of a laboratory by suspending from the center of the ceiling a source and detector at various distances above the floor of a cubic root. The expressions he used for calculating the expected scattering were for an infinite air medium and for the flux of scattered neutrons returning to a source when the source is midway between two non-capturing semi-infinite media, here the malls.

Pleaset (2) developed formulas for the intensity of garma rays scattered by air from a source to a receiver but restricted his analysis to single scattering. He made similar calculations for the intensity of new trons singly scattered by hir from a source to a receiver. He also developed approximate expressions for the reflection of large rays and neutrons from a semi-infinite slab.

As a continuation of this, Pleaset and others (3) illustrated by exact calculations the geometrical effects of the size of a shadow shield and a source on the intensity of garma rays scattered into a receiver.

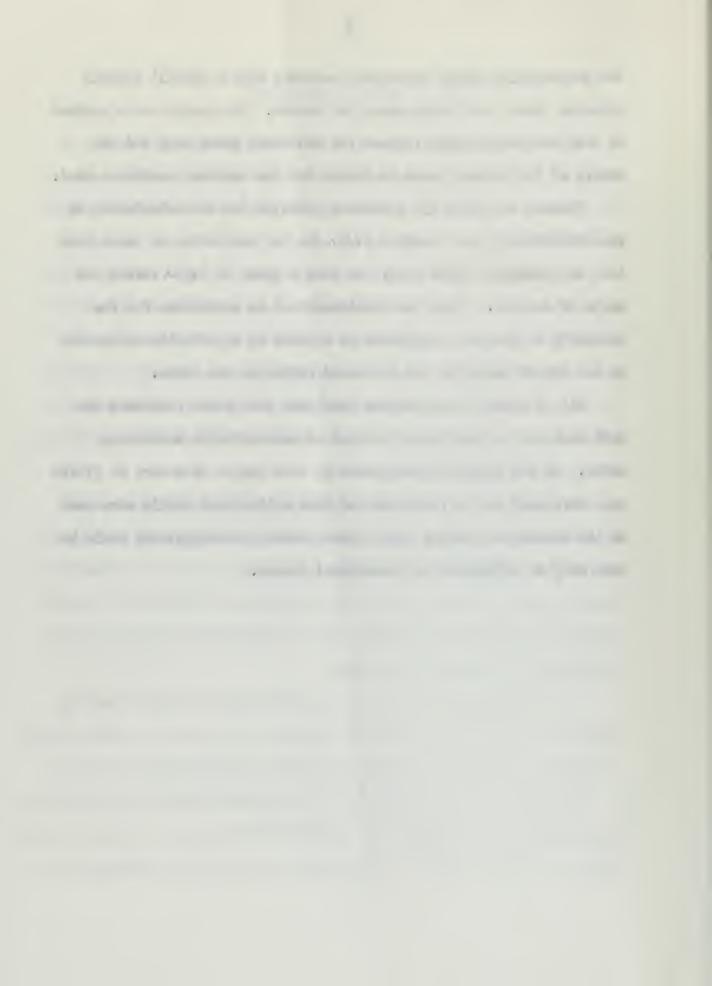
The gumes ray backscattering from various naterials was investigated or existentally and qualita ively by Hine and McCall (h). The exterioral procedure involved placing a point source on or having it suscended over

regard part of the control of the property of the control of the c ____

the horizontally placed scale ring natural with a MaI(TI) or stall detector placed vertically above the source. The results were platted to show the relationship between the scattered game rays and the energy of the primary games radiation for the various geometries used.

Placet and Cohen (5) presented formulas for the calculation of the differential cross section do/da for the scattering of garna rays into an element of solid earle and gave a graph of do/da versus the angle of scatter. Also, the development of an expression for the intensity of the garna radiation at a point in an infinite medium due to the direct radiation and scattered radiation was given.

All of these in cetigations were made with point receivers and with what can be considered infinite or semi-infinite scattering media. In the problem investigated in this thesis detectors of finite size were used as the receivers and thin cylindrical shells were used as the scattering medium, thus, these related investigations could be used only as references and occasional guides.



INI. SCOP OF INVESTMENTOR

The scattering of neutrons and come rays by thin cylindrical shells was investigated analytically and an attempt was made to verify these results by experimental means. The analytical investigation was made for point sources of radiation and finite size detectors, with the source positioned vertically below the center of the detector and with the center line of the detector coincident with the center line of the eylindrical shell.

imperimentally, the scattering of neutrons and game rays by 24ST and Alched 24ST aluminum alley cylindrical shells was investigated. However, the experimental results were overshadowed by the relatively large statistical deviations that were introduced when correcting the experimental results for the scattering of the radiation by the air and the room.

Attempts to reduce this extremeous scattering to an acceptable level were unsuccessful. Thus, the experimental results with the exception of a few of the carra ray readings neither proved or disproved the analytical findings. The few exceptions noted only tended to and support of the analytical results and no positive conclusions could be drama.

and Second Community and the community of the community o , Down being 2 and married to the comments. *

IV. 1 Could to I. ALALYSIS

A. Assumptions

The theoretical analysis of this problem concerning similitude in neutron and gas as rag scattering would have been extra ely complicated without certain simplifying as settions. These included the following.

It was as uped that the sources of radiation were point sources and that the neutrons or gath a rays were emitted isotropically. This is a valid assumption for very small finite sources. If the finite source cannot be considered very shall, but is still small compared to the size of the scattering material, it can be approximated by a suries of point sources.

Any scatterin, or absorption of neutrons or attenuation of are rays by the air was assumed to be negligible. That this is a valid assumption for neutrons follows from the magnitude of the probability that a neutron will be scattered or absorbed in air. The probability that a neutron will penetrate the air or other natural a distance x without being scattered or absorbed is $e^{-\sum x}$ where \sum is the macroscopic cross section for the event in question.

For a substance composed of more than one element Σ is calculated by usin; the formula

$$\sum_{n} \sum_{n} \sum_{n$$

the sale and the sale and the sale and the sale and A STATE OF THE PARTY OF THE PAR where

p is the density of the substance N is Avoradro's number

- f is the weight fraction of the ith element of the substance
- is the microscopic cross section of the ith element for the event in question

A, is the atomic weight of the its element.

For air at standard conditions, the value of Σ_s (scattering cross section) as calculated with this equation is 4.5×10^{-1} cm. $^{-1}$ and the value of Σ_s (absorption cross section) is 7.2×10^{-5} cm. $^{-1}$.

The maximum neutron path length from the source to the detector in this experiment was approximately 65 cm. Thus, the probability that a neutron would be scattered by the air in this experiment was about 0.03 for the maximum distance and considerably less than this for the minimum distance. The probability that a neutron would be absorbed was approximately 0.005 for the maximum distance. These probabilities are for thermal neutrons. As the neutron energy increases Ξ_{0} remains about constant and Ξ_{0} is remaded considerably, so the absorption probability will be less than 0.005 for higher energy neutrons.

That the attenuation of park rays by air is ver, small can be seen by applying the factor e^{-AR} value is the probability that a park ray will penetrate a distance x into a medium without being involved in any reaction that contributes to its attenuation. The total absorption coefficient a is the sum of the absorption coefficients for photo-electric effect, Compton scattering, and pair production. For edr, M

Particular to the second of the second and the same of th The second secon U. gala and an annual rate of the contract of

varies between approximately 1 x 10⁻¹ cm. ⁻¹ for 0.5 Nov game rays and 0.40 x 10⁻¹ cm. ⁻¹ for 4 Nov game rays (5). Therefore, the probability that a gamma ray within this energy range would be attenuated by the air was about 0.0005 to 0.0026 for the maximum distance involved in this experiment.

Another assumption used concerned the number of scattering collisions undergone by each neutron in the 25ST aluminum or Alclad 25ST aluminum cylindrical shells. It was assumed that each neutron that as scattered was involved in only one scattering collision. A consideration of the near free path for neutron scattering λ_s in 25ST aluminum alloy or Alclad 25ST aluminum alloy shows that this assumption is valid. The mean free path λ_s is equal to $1/\Sigma_s$. Equation (1) was evaluated to find Σ_s .

the density of 2457 wrought aluminum alloy is 2.77 gross per cubic em. and its nominal composition (') is 4.5 per cent copper, 0.6 per cent manganese, 1.5 per cent magnesium, and 93.4 per cent aluminum with its normal impurities. These normal impurities and the permissible maximum of each are 0.5 per cent iron, 0.5 per cent silicon, 0.1 per cent mine, and 0.1 per cent c. remium. The cladding mat riel, which is nominally 5 per cent of the total trickness of sheet 0.004 inch or over in thickness and 10 per cent for sheet less than 0.004 inch thickness, has a density of 2.71 grams per cubic cm. Its nominal convosition is 99.3 per cent minimum aluminum with impurities of 0.7 per cent maximum iron plus silicon, 0.1 per cent maximum copper, 0.1 per cent maximum iron plus silicon, 0.1 per cent maximum copper, 0.1

Assuming that the arount of the impurities present is one-half

» • 7,170



NAME AND ADDRESS OF TAXABLE PARTY. THE PARTY OF TAXABLE PARTY OF TAXABLE PARTY OF TAXABLE PARTY OF TAXABLE PARTY. 4 A SHARE THE RESIDENCE OF THE PARTY OF THE PA Hilliam III . I feel to the contract of the co AND DESCRIPTION OF THE PARTY OF and the property of the same o of the regime, $\Sigma_{\rm S}$ for the median is 0.065 cm. 1. Thus $\lambda_{\rm S}$, which like $\Sigma_{\rm S}$ regime approximately constant with increasing neutron energy, is 10.6 cm. for the alloy and 11.76 cm. for the eladding. These values when compared with the neutron a fective thickness of the material considered in this experiment, which is about 0.62 cm., show that the assumption of only one collision for each neutron scattery should not have introduced any great error.

would only be true if the mass of the scattering mucleus was much larger than the mass of the neutron. I measure of the emissive y of the neutron scattering is the average cosine of the sorthering angle in the laboratory system. Classical and Idland (7, p. 97) above that this average cosine for neutrons will emergical less than a few Nov is given by the equation

where A is the mass number of the seat oring raterial. All was number of the allow, which is the sum of the weighted asc numbers of the constituents, is 21.89. In a smaller number is 27.10. In s, $\cos \Psi$ is 0.0231 for the allow and 0.0256 for the claddin which indicates that the emisstropy is relatively low.

The slowin cours of fast now rons is the almost entirely to

4 the state of the s

elastic scattering of the neutrons upon collision with nuclei of the moderator, therefore, it was ensured that all the collisions in the scattering material were elastic.

mes assumed to be small compared with the scattering cross section.

Actually, since the absorption cross section for most elements decreases fairly repidly with increasing neutron energy, this assumption would be of little concern in the deal min, of shielding that must protect personnel from structurally scattered neutrons. Any shield that would protect them from fast neutrons would be effective a minst slow neutrons. Therefore, only calculations for fast neutron scattering would be necessary and in this energy range the absorption cross section is, with for exceptions, much smaller than the scattering cross section.

If for some reason the number of scattered slow neutrons must be known, this can be estimated outto accurately by slightly modifying the equation developed for fast neu rons. This modification is given at the end of the development of the fast neutron scatterin equation.

The mean free path for neutron scattering λ_s is actually a function of energy. If the source of neutrons is not measuremented, this introduces another variable. However, λ_s is practically a constant for neutrons up to about 8 or 10 FeV and, therefore, it was assumed that a constant value could be used for a polyenergetic source of neutrons.

t . 4 •

The differential cross section $d\sigma/d\Lambda$ for monomorpoint game ray sea thring is a function of the angle of scattering. However, calculations show (5) that this is practically constant for angles of seatering pre-ter than about 70 degrees. In this investigation, the angle of scattering, with few exceptions, was precter than this, thus a constant value was assumed for $d\sigma/d\Lambda$.

B. Heniron Sectioning

rigure 1 is a sketch of the system investigated. The scatt ring natural comprises a cylindrical shell of radius r, thickness t, and help ht h, one-quarter of which is shown. The counting tube with an active volume of radius a and help ht h and the point source are positioned on the center line of the cylindrical shell with the center line of the counting tube coincident with that of the shell. The top of the active volume of the vertically suspended counting tube is on the same horizontal level as the top edge of the scattering material. The point source is located on a horizontal line unich is a distance h from the top edge of the scattering material and a distance h from the bottom edge.

The equation which gives the number of neutrons that are singly scattered by the cylindrical shell into the counting tube was developed as follows.

The neutron flux ϕ which reaches the element of volume at P a distance r_1 from the source (Figure 1) is

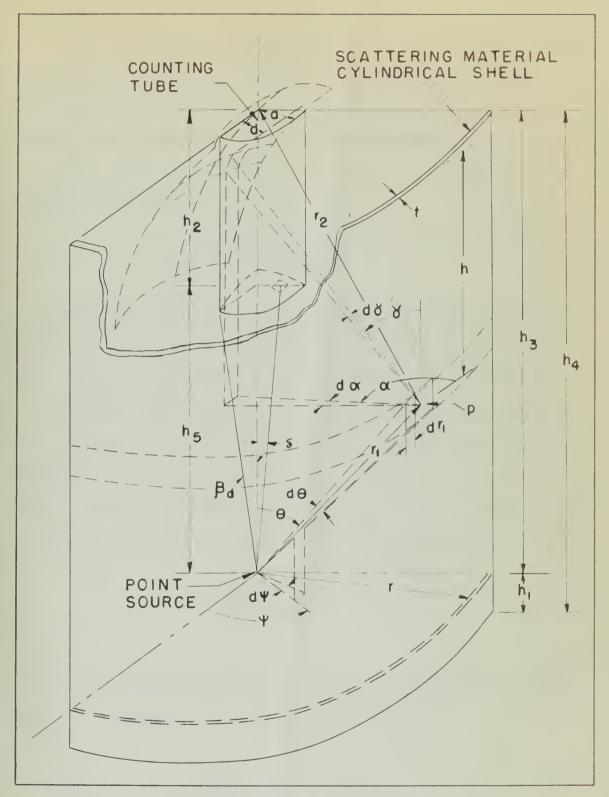


Figure 1. Geometry of scattering.



where Q is the source strength in neutrons per second.

the effective volume element at P normal to the path of a radially emitted neutron is

A radially emitted neutron travels a distance dr within this volume element. To determine the probability of a neutron being scattered while traveling this distance, the mean free path for scattering $\lambda_{\rm S}$ was used. This, the reciprocal of the macroscopic scattering eross section $\Sigma_{\rm S}$, is the average distance a neutron travels between collisions. Thus, the probability that a neutron will be scattered while traveling the distance dr is dr/ $\lambda_{\rm S}$ and the probability p that the neutron will be scattered within the volume element is

Therefore, the member of neutrons n which are singly scattered within this volume clement, which is Equation (2) times p, is

$$dn = 0 \quad d \theta dr d \Psi \tag{3}$$

. لد

sentimed neutrons that are confused toward a point detector is 1/l π r_2 where r_2 is the distance from the volume element to the point reference. However, with the pointer of the problem that was inventionated here, the counting who could not be regarded as a point detector. Instead, the ratio of the solid angle α subtanded by the detector, as viewed from the element of volume, to the total solid angle on μ π steradians had to be used.

This solid angle can be to be found by considering a spherical surface (see Figure 1) which passes through the center of the top of the country, tube and is sen rated by ominging an are of radius r_2 entered at the volume element. Let by setting the proper list as on \sim and δ , the solid on le subtanted by the counting tube can be determined.

ie colid engle A is

$$\Lambda = \int_{X_1}^{X_2} \int_{X_1}^{X_2} X \, dX \, dX \, dX \, dX$$
(1)

where subscripts 1 and 2 sugnify, respectively, minimum and assimum.

The limits on \propto and Y are interdependent in a retain condicated why cas to the shape of the counting take. To avoid this condication and of arrive at an equation rule limits on \propto are set at

These limits on \propto are independent of the other engles, thus, Equation (4) becomes upon integration over \propto and substitution of these limits

$$\Lambda = 2 \tan^{-1} \frac{a}{r} \int_{1}^{8} \sin^{8} x \, dx \qquad (5)$$

appeared. For instance, if $\frac{1}{2}$ is taken to be set $\frac{1}{2}$ the appeared. For instance, if $\frac{1}{2}$ is taken to be set $\frac{1}{2}$ the appeared. For instance, if $\frac{1}{2}$ is taken to be set $\frac{1}{2}$ the solid angle. On the other hand, if $\frac{1}{2}$ is taken to be set $\frac{1}{2}$ (r-a)/h, the solid angle would include some volume outside the counting tube. The same reasoning would apply to $\frac{1}{2}$ then h is less than h. When h is greater than h, a value of set $\frac{1}{2}$ then h is less than h. When h is greater than h, a value of set $\frac{1}{2}$ then h is less than h. When h is greater than h, a value of set $\frac{1}{2}$ then h is less than h. When h is greater than h, a value of set $\frac{1}{2}$ then h is less than h. When h is greater than h, a value of set $\frac{1}{2}$ then h is less than h. When h is constant would not include all the bottom surface of the counting tube in the solid angle. As a compresse, the limits on $\frac{1}{2}$ were taken in two parts and were set by using the distance r minus d, where d is the mean integrated sevichord. This is found from the equation

- AT - 17 and the state of t 7

.lmo

then the lifties are

$$Y_{1} = \cot^{-1} \frac{h}{1 + 1} \qquad (all h) \qquad (6)$$

$$\gamma_{21} = \cot^{-1} \frac{h - h_2}{2}$$
 $(h \le h_2)$ (7)

$$\gamma_{22} = cob^{-1} \frac{h+h_2}{r+d}$$
 $(h \ge h_2)$ (0)

The contribution of the bottom of the detector to the solid angle is included by making the denominator of the laster limit r+d.

These limits on X are independent of Y, but are dependent on θ being related through h by the equation

$$h = h_3 - r \cot \theta \tag{9}$$

Equation (5) gives the could angle subtended by the counting tube. This divided by the total solid angle μ standians is the proportion of scalt red neutrons that will pass through the counting tube volume.



The number of neutrons scattered within the volume element is given by Equation (3), thus, this times the above ratio is the number of neutrons no that are scattered into the counting tube by the volume element. So

$$\int_{0}^{h_{s}} dn = \int_{0}^{h_{s}} dn = \int_{0}^{h_{s$$

The limits on Ψ are zero and 2π and the limits on r_1 are $r/\sin\theta$ and $(r+t)/\sin\theta$ where t is the perpendicular thickness of the scattering raterial. Integrating over r_1 and Ψ and substituting the limits give

$$n_{s} = \frac{\text{Ot}}{8\pi \lambda_{s}} \int_{\theta_{1}}^{\theta_{2}} \left[2 \tan^{-1} \frac{2}{s} \int_{\chi_{2}}^{\chi_{2}} \sin \chi \, d\chi \right] \frac{d\theta}{\sin \theta} \tag{10}$$

Integratin, in this equation over Y and substituting the limits (Aquations (6), (7), and (8)) and then substituting for a from Equation (9) result in an extremely condicated and lengthly integral of θ . To arrive at a simpler but still a good approximate expression for n_s , the bracket of Equation (10) which is the integral equation for Φ was replaced by the average value of Φ . This average value is found as follows.

countion (5) is integrated and the limits as given by Rustions (6),

(?), and (i) are substituted. I is gives

$$\alpha = 2 \tan^{-1} \frac{a}{r} \left[\frac{h_2 - h}{\sqrt{(h - h_2)^2 + (r - c)^2}} + \frac{h}{\sqrt{h^2 + (r - c)^2}} \right] \qquad (h \le h_2)$$
(11)

$$\Delta = 2 \tan^{-1} \frac{a}{r} \left[\frac{h_2 - h}{\sqrt{(h - h_2)^2 + (r + d)^2}} + \frac{h}{\sqrt{h^2 + (r - d)^2}} \right] \qquad (h \ge h_2)$$
(12)

The values of \boldsymbol{a} throughout the range of h are found for the geometry involved by assigning values to h, say n_0 , n_1 , n_2 ,..., n_1 ,..., n_k . These values run from zero to h_k (Figure 1) and are equally spaced, the distance between them being b. Then the average value of \boldsymbol{a} , say $\boldsymbol{\bar{a}}$, is found from the equation

$$\frac{1}{\sqrt{2}} \int_{0}^{2\pi} \int_{0}^{2$$

Talues of $\overline{\Lambda}$ for the various geometrico used in this investigation are plotted in Figure 2.

Using this average value of A , Lamation (10) can be written



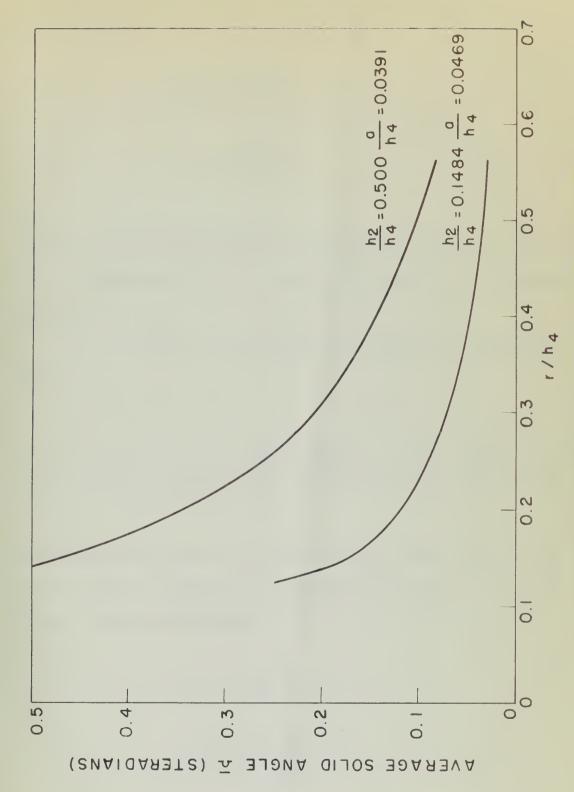


Figure 2. Average solid angle for various geometries.



From Figure 1, it is some that the limits on θ are

$$\theta_2 = \cot^{-1}\frac{h_3}{x}$$

was re h, is considered positive if the bottom edge of the cylindrical shell is horizontally above the source and negative if the bottom edge is tolow the source.

The integration of equation (14) and substitution of the limits THE WALL

$$n_{s} = \frac{\sqrt{2}}{\sqrt{1 + \left(\frac{h_{1}}{2}\right)^{2}}} - \ln\left(\sqrt{1 + \left(\frac{h_{3}}{2}\right)^{2}} - \frac{h_{3}}{2}\right)$$

Referring to Figure 1, it is evident that h /r is the tengent of the backward angle at the source and ha/r is the tangent of the forward angle. Thus the substitution of

$$\tan \beta_1 = \frac{h_1}{r}$$

ton
$$\beta_2 = \frac{\mu_2}{\pi}$$

and con ination of the natural le, terms gives

$$\frac{\sqrt{1 + \tan^2 \beta_b} - \tan \beta_b}{\sqrt{1 + \tan^2 \beta_b} - \tan \beta_b}$$

$$\sqrt{1 + \tan^2 \beta} = \frac{1}{\cos \beta}$$

and
$$\tan \beta_b = \frac{\sin \beta_b}{\cos \beta_b}$$

so that the numerator of the natural log in the above equation can be written $(1-\sin\theta_b)/\cos\theta_b$. A similar expression can be substituted for the denominator to give

$$n = \frac{\sqrt{\pi}t}{8\pi\lambda_{8}} \ln \left[\left(\frac{1 - \sin\beta_{b}}{\cos\beta_{b}} \right) \left(\frac{\cos\beta_{f}}{1 - \sin\beta_{f}} \right) \right]$$

The final expression for n is found by letting

$$H = \ln \left[\left(\frac{1}{2} - \sin \beta_0 \right) \left(\frac{\cos \beta_1}{2} - \sin \beta_1 \right) \right]$$



so that

This equation gives the total nation of neutrons per second that are simply scattered by the cylindrical shell into the counting tube volume. Then evaluating H, it must be remembered that h₂ is considered positive if the account edge of the cylindrical shell is horizontally about the source and negative if the bottom edge is below the source. Therefore, $\beta_{\rm b}$ and, consequently, sin $\beta_{\rm b}$ are positive for the first mentioned conditions and negative for the latter. A plot of H versus $\beta_{\rm b}$ for vertoes values of $\beta_{\rm c}$ is given in Figure 3.

The lotal major of fact neutrons that are cingly scattered if q is reactined as the fact neutrons for second emitted by the source. A possibility for the med of a chight medification to this equation arises from the fact that a small fraction of the fact neutrons emitted at energies just above thermal are reduced to thermal energies upon colliding with the medica of the structural material.

the energy E of three neutrons after the collision is related to

* .

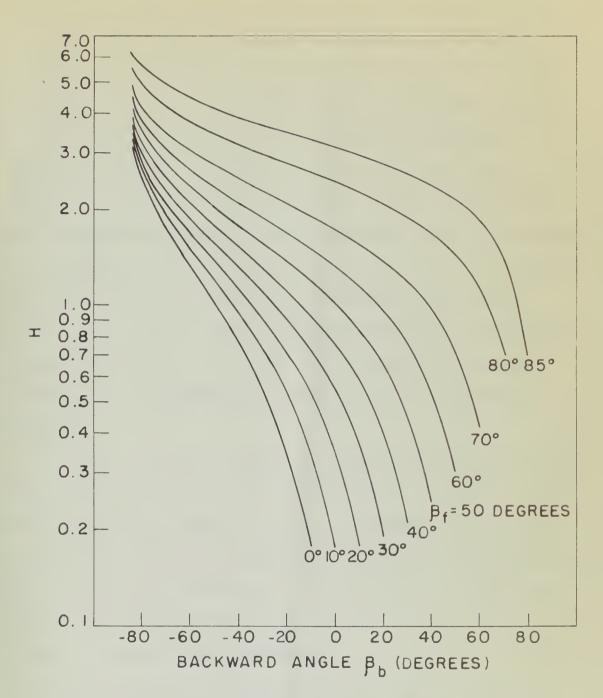


Figure 3. Variation of H with geometry.

* . i i

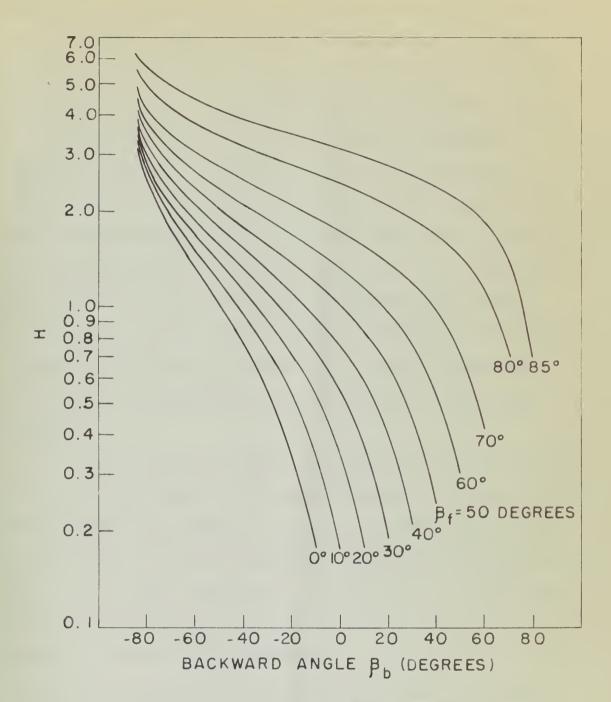
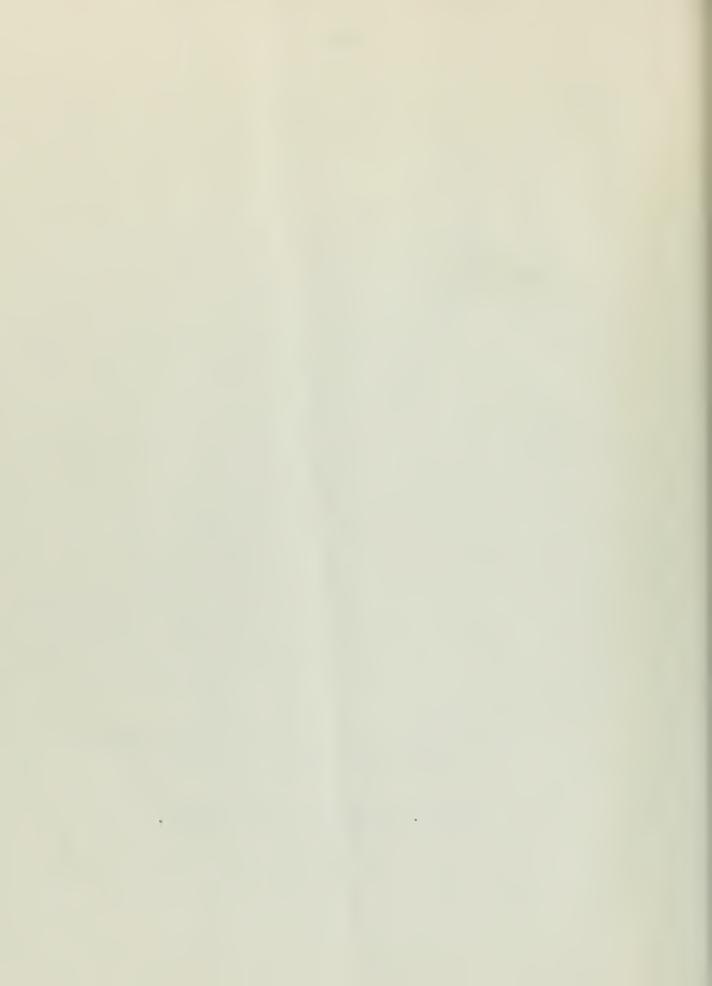


Figure 3. Variation of H with geometry.



where A is the mass number of the scattering a sortal and ϵ is the scattering angle. Since the neutrons of interest here are those scattered into the thermal energy region, the surge of the mal neutrons.

In this investig tion or in similar setues with shells of scructural natural, the scattering angle has an average value of about 90 degrees. For this scattering angle and 2h5T aluminum alloy 12, using the above equation, is equal to 0.935 L. Thus, on the average, these neutrons emitted by the polyenergetic source in the energy range from E_t to 1.07 E_t are scattered into the thermal neutron energy region. For example, if morral neutrons are defined as those with an energy of 0.25 ev or less, the neutrons with energies between 0.25 and 0.268 ev are scattered upon collision into the thermal energy region.

For alrost all neutron sources, the number of neutrons ordered in this very narrow energy band are a minute fraction of the total neutrons emitted. Monce, for practical purposes, all neutrons emitted as fast (slow) neutrons can still be considered as such after they are sattered.

Las, Equation (15) is applicable to fast neutrons, as are the succepturent equations given in this section, if Q is the marker of fast neutrons per second exitted by the source.

Other necurements of the scattering by the cylindrical shells would be the ratio $R_{\rm S}$ of the neutrons scattered into the counting tube to those that reach the counting tube directly or the ratio $R_{\rm T}$ of the total neutrons that reach the counting tube to those that proceed

.

and the second s and the first term and the second w 8 directly.

The upper of neutrons the arrive directly is the point source strength C times the ratio of the volid angle subtended by the end of the counting tube to the total solid angle h π sterediens. The solid angle subtended by the bot on of the quarter of the detector shown on Figure 1 is

$$\Lambda = \frac{\pi}{2} \int_{\xi_1}^{\xi_2} \sin \xi \, d\xi$$

in. Limits on 8 are zero and cot 1 h,/a, thus

$$\Lambda = \frac{\pi}{2} \left(1 - \frac{h_2}{\sqrt{h_2^2 + a^2}} \right)$$

The solid angle a sucturied by the bottom of the detector is four thes this, or

$$\Delta_d = 2\pi \left(1 - \frac{h_5}{h_5^2 + a^2}\right)$$

The proportion of the same , utrons which arrive directly at the detector is $\Lambda_d/k\pi$, so the number n_d of source neutrons that arrive directly is

$$n_{d} = \frac{Q}{Z} \left(1 - \frac{h_{5}}{\sqrt{h_{5} + e}} \right)$$

The term in the parenthesis can be written as

,

The state of the s

(100/-1)-11-1

(T. J. ...) != /

where (see Figure 1)

$$\frac{a}{h_s} = \tan \beta_d$$

Su officing from this relationship for a/n, and then substituting $1/\cos\beta_d$ for $\sqrt{1+\tan^2\beta_d}$ gives the final expression for n_d. Thus,

$$n_d = \frac{1}{2} (1 - \cos \beta_d)$$
 (16)

The scattering ratio R was previously defined as n_g/n_d (Equations (15) and (26)). So

$$\frac{R}{S} = \ln \pi \lambda \left(1 - \cos \beta_{0} \right) \tag{27}$$

the total ratio R was a vicusly defined as $(n_s + n_d)/n_d$ which equals (n_g/n_d) + 1. Thus

$$R_{T} = R_{S} + 1 \tag{16}$$

Inations (17) and (18) can be applied to the total neutrons from a polyenergetic source or to the fast neutrons from a polyenergetic source. In sc equations can also be applied to the arribations if the cross section for accomption is negligible compared to the cross section for scattering. Under similar circum-



stances, Equation (15) can be sed provided Q is the thermal neutrons per second emitted by the source.

If the absorption cross section is not negligible constraint to the scattering cross section, but is still screenal less than the scattering cross section and, if the thickness of the cylindrical shells used is small conserve to the constraint for absorption (which it rust be for Equation (15) to be walld), a good first approximation of the thornal neutron scattering our be calculated as follows.

The fraction of normally incident Lernal neutrons that would be absorbed in the shell, if the scattering cross section were negligible, is $(1-e^{-\sum_{a}t})$ there \sum_{a} is the macroscopic absorption cross section and t is the thickness of the shell. This fraction times brustlen (15) gives a good first approximation of the number n_{p_q} of thermal neutrons scattered by the cylindrical shell into the counting tube volume. Thus

$$n_{S_{t}} = \frac{C \pi t T}{8 \pi \lambda_{S}} \left(1 - e^{-\sum_{s} t} \right)$$
 (19)

Agrations (17) and (18) are, for this case,

STR.

$$R_{T_{\xi}} = R_{S_{\xi}} + 1 \tag{23}$$

. (1-12)

is the major of hornel neutrons to second emitted by the source.

C. Ga a lay Coastering

The geometry for gare ray scattering as the same as that for neutron scattering (ligare 1) and the development of an equation for monoconceptic garmany scattering is similar to the development of the equation for neutron scattering.

If it is assumed that no attraction of the para rays occurs in the air, the para ray flux θ_y wide reaches the element of volume at P a distance r_y from the source is

The effective volume element at P is

The differential cross section d σ /d Λ for garma ray scattering, which has units of per incident photon per electron per cm. 2 per storadism, is the probability that a garma ray will be scattered through an angle ϵ into the element of solid angle centered about ϵ . This cross section times the number of electrons η in a cubic on, of the

v | the second secon > of a photon being singly scattered through the angle & into the element of solid angle centered about & while within the volume element.

Consequently, the major of games rays as sestioned while within the volume element is the flux at the element times the probability of scattering within the element, or

The number of gard rays n_{s_s} which are scattered into the counting tube volume is the above equation multiplied by the solid angle surtended by the countin; tube as seen from the volume element. This solid angle is given by Equation (h). To avoid the difficulties identical to those encountered in the neutron scattering equation development, the solid angle subtended by the counting tube was replaced by the average angle \bar{a} . Equations (11), (12) and (13) are used to calculate \bar{a} . Values of \bar{a} for the various geometries used in this investigation are plotted in Figure 2.

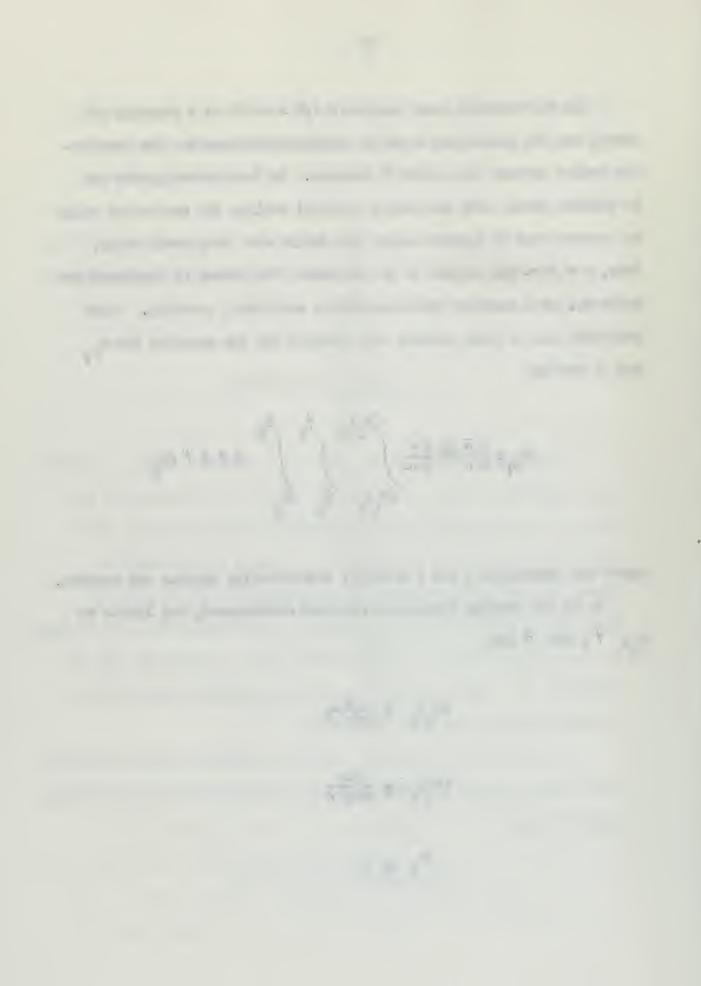
The number of game rays n_{S_8} which are scattered into the counting tube volume is found by multiplying the above equation by this average angle. Thus,

· the first limit (LC) has been party and the contract of the _0 he differential cross section do /d n which is a function of energy and the scattering angle is approximately constant for scattering angles greater than 70 degrees. In this investigation and in similar setups with scattering material shells, the scattering angle is prester than 70 degrees except for shells with very small radii, thus, do /d n was assured to be constant. The number of electrons per cobic cm. is a constant for a particular scattering raterial. These constants can be taken outside the integral and the equation for n a constant of materials.

$$n_{s_{\xi}} = \frac{s \bar{n}_{n}}{4 \pi} \frac{d\sigma}{dn} \int_{(r_{1})_{2}}^{(r_{1})_{2}} \int_{1}^{\psi_{2}} \frac{\partial}{\partial t} d\theta d\psi dr_{1}$$

in we the subscripts 1 and 2 signify, respectively, minimum and numbers. As in the neutron scattering of a tion development, the limits on ${\bf r}$, ${\bf r}$, and ${\bf \theta}$ are

$$(r_1)_1 = \frac{r}{\sin \theta}$$



$$\theta_2 = \cos^{-1} \frac{h}{r}$$

In the latter limit, h is considered positive if the bottom edge of the cylindrical shell is horizontally above the source and negative if the bottom edge is below the source.

Integrating and applying these limits gives the opposition for the number of nonconcriptic country; per second that are singly seat ered into the counting tube volume. This expression is

$$n_{s_{\chi}} = \frac{s_{\overline{\Lambda}} n_{o} t_{o} ds}{2 ds} \left[\ln \left(\sqrt{1 + \left(\frac{h_{\gamma}}{r} \right)^{2} - \frac{h_{\gamma}}{r}} \right) - \ln \left(\sqrt{1 + \left(\frac{h_{\gamma}}{r} \right)^{2} - \frac{h_{\gamma}}{r}} \right) \right]$$

scattering equation development. A plot of II versus β_b for various values of β_s is given in Figure 3. Placing I in the above equation

,

*

the same of the sa

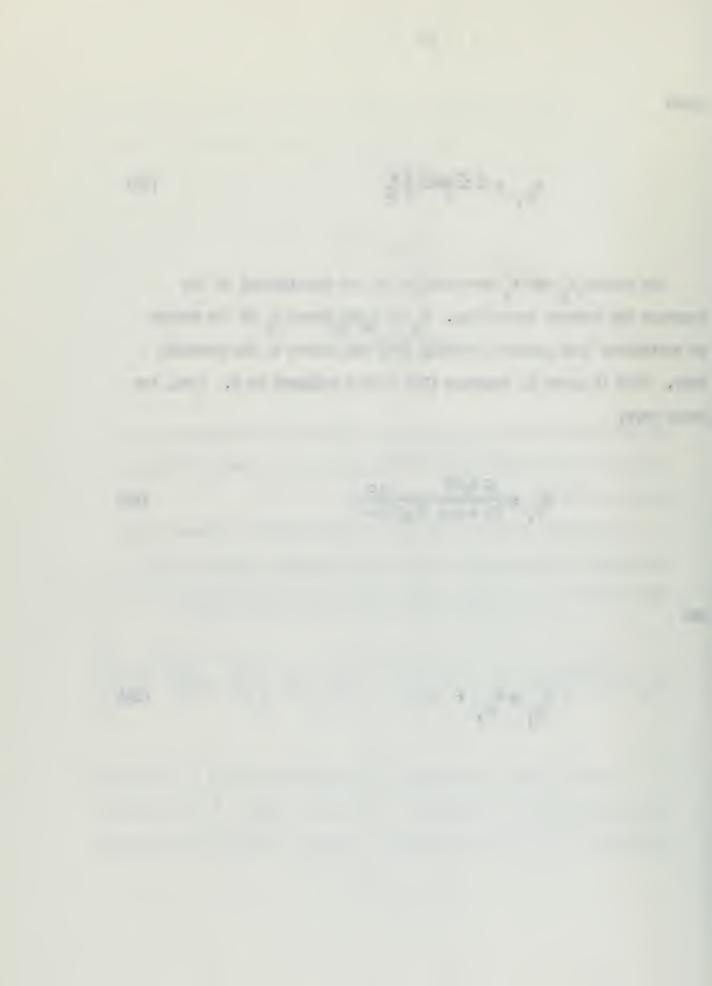
gives

the ratios R_g and $R_{\bar{q}}$ were defined in the development of the equation for neutron scattering. R_g is n_g/n_g where n_g is the number of radiations that proceed effectly from the source to the counting tube. This is given by Equation (16) with Q replaced by S. Thus, for gar a rays,

$$R_{s_{g}} = \frac{\pi n_{g} t H}{(1 - \cos \beta_{d}) d \Omega}$$
(23)

and

$$R = R + 1 \tag{24}$$



V. RILLI BAL PROGRAM

A. "Literials

the materials used in this investigation were 2ht and Alched 2hSr aluminum allog, paraffin, cadmium, loud, plywood, borated send, a neutron source, and a game ray source.

The aluminum alloy was purchased from the Ioum State Gollege
Insurament Shop, the paralfin and plywood were purchased from local
concerns, and the cadmium in the form of 0.010 inch shoot was purchased
from the Division Local Company, Summit, Illinois. The lead and
boroted sand were available in the Laboratory.

A polonium-beryllium neutron source was used. This source is contained in two right cylinders. The outer cylinder has enternal dimensions of 1.0 inch diameter and 1.2) inches height. The dimensions of the inner cylinder, within which the source is scaled, were estimated by comparison with dimensions given by Rausa (1) for the same upper of source. Thus, the inner right cylinder was estimated to have internal dimensions of 0.50 inch dimension and 0.60 inch height.

millicardes, therefore, the strongth at the time of the experiment (May 1950) was approximately like dillicardes. The neutron production from a source of this type is estimated at 2500 neutrons per second per millicarde so the flux from this source was approximately 2.05 x 10⁵ new roms per second. Reuse (1) stated that the superior maximum per deadlike exposure to polonia - perfilier new rows for a 1,0 hour work

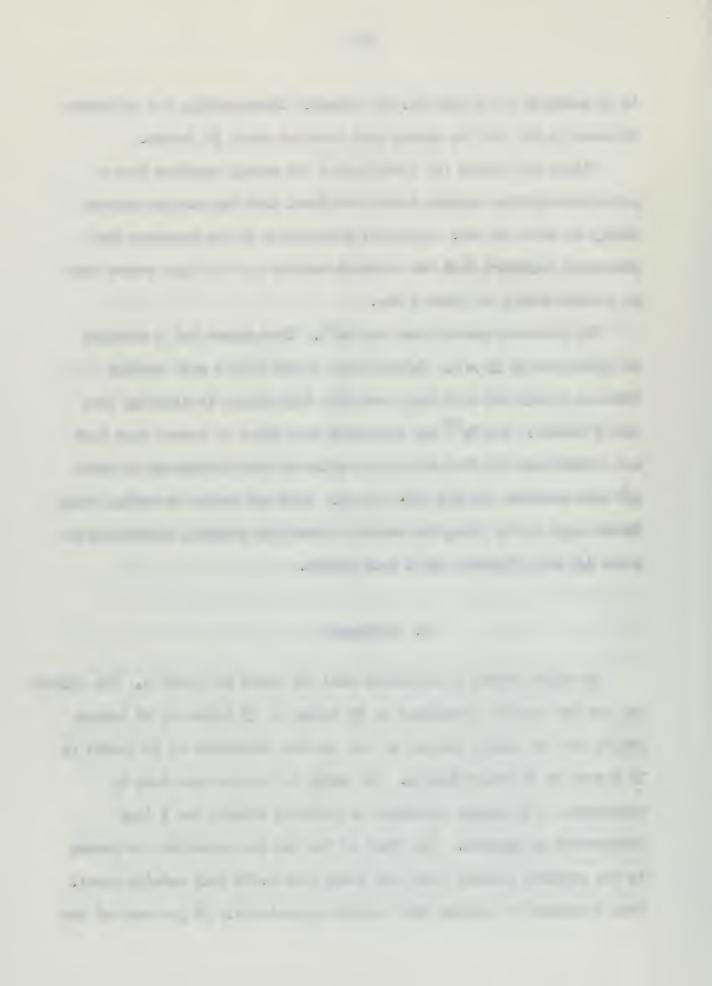
, A is No neutrons per square on. per second. Consequently, the telerance distance in air for the source used here was about 10 inches.

pole dun-beryllium neutron source as found that the animam nection energy is about 12 Nev. A resident integration of the spectra depresented indicated that the neutrons ordered by this type source have an everage energy of about 5 Nev.

Inc parts re source and use Co⁶⁰. This source had a strength of approximately 10 μ c. Colonistiens showed that a safe working distance in air for a h hour work with this source is slightly less than 2 inches. The Co⁶⁰ was conclined in a piece of Scotch tape that was rolled into the form of a right cylinder with distances of about 1/0 inch character and 3/0 inch height. This was scaled by adding other Scotch tape to it, thus, the source as used had external distances of about 1/4 inch diameter and 1 inch height.

. Tourment

ing box has obtained aimensions of 23 inches up 23 inches by 27 inches by 11 inches by 21 inches by 21 inches by 21 inches by 21 inches the light. The malls of the low were rade by cambricals a 13 inches by classes of paraffin beam in two 3 inches the largest of paraffin beam in two 3 inches the largest of the box was recovable for access to the counting charter will a linear with 0.010 inch carrier sheet.





time le a sere de la continua de la secola

3 - Tolor of The

C - of etc and come, some slea ri-

D - Inde or the source in position

I - Just or helding of limit of should

7 - (3. 1. C. 1 1. C. 1.)

I am L'ICEL'S, DOLL TO ELL STONE MONOTOLE





incident neutrons that have energies of 0.25 ev or less which were here defined as slow neutrons. The peraffin-plywood sandwich by moder that any incoming fast neutrons increases the probability of capturin, them in the cadridm. A hole to accommodate the counting tube cable was drilled through the center of the top of the box. Two small eye-hooks were screwer into the top of the charber. The fine cord (approximately 0.018 inch in clauter) that was used for suspending the detector and source was lastened to those hooks.

the 2011 and Alclad 2011 aluminum alloy was rolled into cylindrical shells by he foun State College Instrument Shop. Since smooth shells were desired, a c lon itakinal junction was not riveted or welded but simply held togeth r with scatch tape, except for two of the nearlor gage shells. For the se, one to exceed two outward opring action, fine cord had to be used to hold the junction.

high. Three of these, rolled from 2057 eluminum alloy sheet, had a shell thickness of 0.025 inch and a radius of 3, 4.5, and 6 inches respectively; two, rolled from lokal 2457 aluminum alloy sheet, had a shell thickness of 0.064 inch and a radius of 6 and 8 inches respectively; and two, also rolled from Alchad 2557 aluminum alloy sheet, had a shell thickness of 0.126 inch and a radius of 4.5 and 8 inches respectively.

For neutron counting, the counting elected was composed of a 310 lined proportional counter connected circuit of an electronic scaler. The proportional counter was namulactured by

and the contract of the case that the contract of the contract > General Electric and has a cylindrical active volume of 1.25 inches in diameter by 8.0 inches in length.

A Fodel 200 scalar manufactured by the Radiation Instrument bevelopment Laboratory was used. This model has a built-in amplifying circuit and is equipped with a discriminator, a gain central, a register, and a timer. The input voltage to the scalar was maintained at 115 volts by a "Stabiline" type 155101 voltage regulator.

The operating characteristics of the neutron counting circuit were investigated thoroughly. With the discriminator set at 70 and the pain switch on F, a 25 volt plateau of 2.5 per cent slope was found in the voltage range centered about 675 volts. Thus the operating voltage, discriminator, and pain were set at these values for neutron counting.

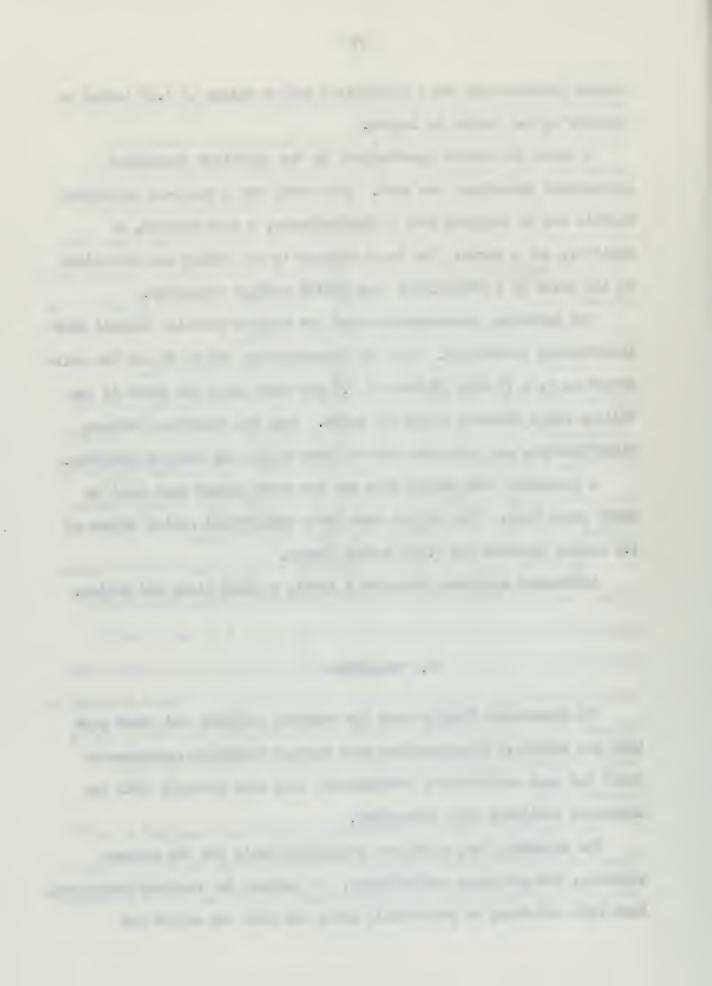
A tracerlab ACS Guiger tube and the above scaler were used to count garma rays. This Geiger tube has a cylindrical active volume of 1.5 inches dismeter and 2.375 inches length.

Adultional equipment included a level, a plumb line, and scalus.

C. Procedure

The procedures finally used for counting neutrons and here rays were the result of experimenting with various stabiling arrangements until the most satisfactory arrangements that were possible with the equipment available were determined.

The shielding box, which was explicitly built for the neutron counting, did not prove satisfactor. It reduces the neutron background, both fast and slow, to practically zero, but with the source and



chades of in the best, its pent of some neutrons (really evershades i is value as a shield a new fast and show neutrons
including on the outside of the best. With the same superal his
inches below the detector, the new ron count in the best neutron
approximately 20 times he count outside the best and the shes neutron
count of a precimately triple. The force, the neutron country was
come outside the box.

A few emploratory counts that the box showed that the scuttering free the circumstant the room was lower with the source submitted some circumstant to the floor. Thus, the cap rimental arrange into mean in Figure 4 resulted.

The Mieldin box, as expected, we found to be ineffective as a new roy stield. The shielding we ried available included 10 pieces of local each with elementions of about 1 inch by 8 inches of 16 inches, 23 pieces or local each with dimensions of about 3/4 inch by 1 and 3/4 inches of hinches, and 2 boxes at 12 be s of occurs or at ever in about 10 inch in the amount.

of the larger pieces of 1 were placed on the floor of the counting chart r to determine the effectiveness of the lead in reducing the real sector in caused by the eir of the room. This errange is did not noticeably reduce the scult ring. In det, while these we deces of lead in relation and all the residual available lead and he corated sand placed next to the outside of the box, the count still was not noticeably reduced. Therefore, the real arry counting was done cutoide

. . -----* 11 2-2 principal to the first the same of the sam the state of the same of the s from the air and room could be an rielly released over chalar scatterin inside the box. These explentary counts indicated that the
distance the source and detector we placed above the floor of the
room of not incluence the state wire appreciably, and that the
searce of not incluence the the mind appreciably, and that the
searce of the test just above the floor with all the available had placed
below the . The best arrangement was found to be 1) inclue by 16
inclue by 16 duchos of lead constrol directly under the counter and
a tree with the remaining our law pieces of lead placed flat on the
floor one on each of the four side, of this control error, intend
with the 2) smaller pieces of 1 m based in the space but in these
outer blocks.

country was similar to take a sm in right be copt, a course, who

count and one other count made to determine the number of blow neutrons being seart red by the cir and the room into the detector, were taken with the detector covered with 0.010 inch of cadmium. This thickness of a drive will conture approximately 98 per cent of the incident neutron that have carrie of 0.2; ever less. Since any neutron with an energy higher than take at considered to be a fast neutron, the counts that the detector covered when due to fast neutrons. Only fast neutron counts were taken because precipally all to heatrens

The second secon HI NOTE THE RESERVE OF THE RESERVE O orivini , source of this ope are lest a virous.

Since the results of this investigation depended to a great extent on the correctness and declication of geometrical arranges ats, every effort was made to accure such conditions for both the neutron and the ray measure sits. The procedure in one case was in rule il.

(as reclinately 0.015 inch in discret) which were fastened to four eyehooks scrowed into the upper side of the cross bar of the suspension
agracius. The cords were secured in a namer that would allow the
distance between the detector and the cross bar to be either shortened
or languaged by simply turning the books in the proper direction.
This is that was also used to writefully align the councing tube. The
distance he between the top of the active rolume of the sounting tube
and the local blocks in the case of grams ray counting or the stand for
holding the cylindrical shells in the case of neutron counting was
carefully measured with a real uning stick. The vertical all ment of
the counting tube was cicaled with a lever and also by sightly along
a plant line that was suspended behind the apparatus. The back round
counts was rade with the counting tubes suspended in this position.

the source was suspended below the detector by a piece of fine cord which was fastened at each and to another piece of cord that was placed around the detector just bowt its better edge. The distance he between the source and the bottom of the active volume of the detector was resource and then a collect by measuring the distance the source to the lead blocks in the case of great ray counting or the

. · ANY AND DESCRIPTION OF THE PARTY OF THE PART The second of th The distances were sensued from the vertical mid-point of the source of the form the dissert is shown in the previously. The entering of the source halow is detector as checked by placing the level vertically along the distance of the projected must the position of the source on the first the horizontal particle pass the position of the source.

I represent and not lest end slow neutron count were name to the power of the source and a tector in position. These counts were made for such also of hy used and, were counted for the scale with caused by the six and room, they are the counts due to the radic ion that process directly from the source to the director.

restrict the proceeds frostly on that that is scattered into the detector by the alterium alka evaluational should, the wells were positioned around the source had betector. The center line of these altiquent was checked by reasonable to a distance from an detector tall to the should at various position around the periodicry of the shell. Therefore, the checked of measuring around the periphery of the shell could not be followed, therefore, the seven different extincted shells used were positioned with the natural detector was control to a shell used were positioned with the seven different extindrical shells used were positioned with the neutron detector undo and, suitable nor if you are the same that

A STATE OF THE PARTY OF THE PAR and the second s PARTIES AND ADDRESS OF THE PARTIES AND ADDRESS O where the same of THE RESERVE AND ADDRESS OF THE PARTY OF THE the distance of the second sec the shells then the detector was covered.

whichested horizontal never at a the alignment poper, the stand, or the datester, or the possibility of the detector and source not remaining aligned with the true verticel. An attent was made to eliminate those possibilities by making the operatus concerned as secure as possible. Furthermore, to be sure that the geometry remained the came during the counts, the vertical alignment of the B¹⁰ tuke was cheshed before it was covered and again after it was uncovared and after the counts were taken the pariting on the piece of paper on the stand were checked by placing one of the calindrical shells in the position indicated by the rations and measuring to determine if the shell was still centered about the detected. Of course this did not exclude the possibility of compensating movements occurring, but such combinations were highly unlikely.

the counts determined by recitionin, each of the cylindrical shells about the source and the detector were corrected for the scattering count was that due to the sun of the radiation scattered into the detector by the shell and the radiation that proceeds directly from the source to the detector.

To correction was made for the secondary effect of the room or air scattered radiation, which correlly returned to the countin tube when the cylindrical shell was not in position, being scattered and from the detector by the cylindrical shell was not in position, being scattered and from the

the base of the second to the and resident day if it is not consider the second s And the second section is a second section of the second section in the second section is a second section of the second section of the second section is a second section of the section o

. . . Cutro : Servicerin;

The experimental results for neutron scattering by the aluminum lies cylindrical shells are listed in Nuble 1. The difference between the first two counting rates listed or both h, equal h inches and h general 3 inches is the counting rate as due to slow neutrons. For 3 inches this difference is 27.3 ± 1.2 and for h inches it is 25.7 ± 1.1. Thus, the slow neutron counting rate as sined practically constant with these two source positions, indicating that all the slow neutrons reaching. The detector were the result of scattering by the sir and room and that none of the slow neutrons are is used directly by the source.

The fast neutron counts iven in Table 1 had to be corrected for the scattering due to the air and room. In makin, this correction it was sent of that the number of fast neutrons scattered by the air and room into the counting tube was not influenced by the alarmon cylinerical shells being present or by a small revenent of the servee.

The regulative of this correction can be calculated from the formula

A STATE OF THE PARTY OF THE PAR , , <u>†</u>

Table 1

r	dinari Janari Janari Janari		h ₅ (in.)	Counting time (minutes)	net counting rate (R) (counts per	llu trons counted
in.)	(in.)	(in.)		-	minute)	- 01
3.5	none none 0.025 0.025	16 16 36	3 3 3 3	40 60 60 60 60	43.0 ± 1.1 16.5 ± 0.5 16.1 ± 0.5 16.4 ± 0.5 16.3 ± 0.5	fast and slow fact fast fast
6 8 4.5	0.06h 0.06h 0.126 0.126	16 16 16 16	3333	60 60 60 60	17.2 ± 0.5 17.1 ± 0.5 17.4 ± 0.6 16.8 ± 0.5	fast fast fast
3 4.5 6	none none 0.025 0.025	16 16	and and their man constraints and annual	40 60 60 60 60	35.h = 1.0 9.7 = 0.h 10.1 = 0.h 10.3 = 0.h 9.5 = 0.h	fast and slow fast fast fast fast
6 8 4.5	0.06l; 0.06l; 0.126	16 16 16 16	There has been bound by and	60 60 60	9.9 ±0.4 9.9 ±0.4 11.7 ±0.4 10.2 ±0.4	fast fast fast

where R, is the lotel fast neutron countin, rate

R is the fast neutron counting rate and to those neutrons that proceed directly from the source to the detector

R, is the fast neutron counting rate due to these no trons that 'P are scattered by the air and the room into the detector.

, . 1,000 . . . * . . AC. 4 - 4 . 4 4 4 4 . - * . 2 , de de . . 100

As the circance h between the source and detector is clarited, in will very according to Eccation (16). This equation is based on the assumption of a point source. Orientations made by replacing the newtron source used here with a series of centrally located point sources showed that this assuration is still valid for values of h equal to 3 inches and h inches.

The ratio of P_{D_F} at $h_{\mathcal{G}}$ equal 3 inches to P_{D_F} at $h_{\mathcal{G}}$ equal 4 inches is then

where $\cos \beta_d$ is calculated from the radius of the detector and the distance h_5 . The radius of the detector used here is 0.605 inch, so that the above ratio is 1.75.

HOW

172161

Dividing the first of those of a lens by the latter, so it to the for the ratio $\left(R_{\rm D_F}\right)_3/\left(R_{\rm D_F}\right)_4$, and recruming results in the equation

production and the second seco 7 - () ()

Tast neutron countin, rates corrected for air and room seattering and total neutron seattering ratios

shell circumions r t in.) (in.)	n ₅	counting rate (1.) (counts per minute)	(coun' per uln te)	P _T exertal	R _T tuco- ratical
none 3 0.025 6 0.025	3 3 3 3	16.5±0.5 16.1±0.5 16.4±0.5 16.0±0.5	15.0±1.3 15.0±1.3 15.7±1.3 16.1±2.3	0.975 to.115 0.995 to.116 1.000 to.116	1.020 1.013 1.003
6 0.064 8 0.064 4.5 0.126 0 0.126	3333	17.2±0.5 17.1±0.5 17.4±0.6 16.8±0.5	16.5±1.3 16.1±1.3 16.7±1.3 16.1±1.3	1.014:0.119 1.030:0.119 1.050:0.120 1.020:0.136	1.020 1.010 1.067 1.020
none 3 0.025 4.5 0.025 6 0.025	and the state of t	9.7±0.h 10.1±0.h 10.3±0.h 9.5±0.h	9.0±1.3 9.4±1.3 9.6±1.3 0.0±1.3	1.064±0.209 1.067±0.211 0.267±0.200	1.0k7 1.023 1.013
6 0.064 8 0.064 4.5 0.126 8 0.126	Project Projec	9.9±0.4 9.9±0.4 11.7±0.4 10.2±0.4	9.2±1.3 9.2±1.3 11.0±1.3 9.4±1.3	1.02210.205 1.02210.205 1.11210.200 1.00410.209	1.034 1.015 1.115 1.035

This equation, upon substituting the fast neutron counting rates without a colindrical shell in position for the two values of h_{μ} used,

have a value of 0.7^{\pm} 1.2 counts per minute for h_{μ} . The fast neutron
counting rates connected for this security, are given in Table 2.

The value of h_{μ} is 16 inches for all the cylinarical shells, Marefore,

, \$ * . . -- L 17, 2 . . . - . à. . . 1,13 4 4 9 7 - a 4 - 4 * * Ł . . E W 1 . . . 4 A. * A 1 44 II, is a . . . - 7 4 U , C . . ė, . 4 , 191 3 4 **5** 29 e 4 4 , , + p 4 že. G Ji . . . A 3 4 . . - . 4 4

the same places in the same of the last through the same of

io is not listed in this table.

The experimental total newtron societies ratios R, as determined by dividing each corrected counting rate when with a cylindrical shell in position by the corrected counting rate when no shell was in position, is also listed. The last column in Table 2 lists the theoretical values of R, which were consisted by using E, which the

Any comparison of the erroric stal results with the theoretical values of R was irrossible due to the statistical deviations in the erroric stal values. This large statistical deviation is for the most per-caused by the deviation in the counting rate due to the scattering from the air and the room. Twent possible effort was made to reduce this unanted scattering to a statistically acceptable level, I wever, these efforts were not successful.

alloy cylindrical stells are list in Table 3. Since h is 16 inches for all the shells it is not list d in the table.

The not counting rates listed in the last column of Table 3 had to be corrected for the postering and to the air and room. This courselled was made in a man r identical to that used for the correction to the neutron counting rates. The games may source was made smaller in dimensions than the neutron source, thus the assumption of a point source, as is required to apply spection (16) to valid.

	120	

Carm ra, counting rates cornered for air and room sect orin and total game ray sectioning ratios

Table h

100 10 10 10	rical II Dions	hg (in.)	net counting rate (1) (counts per	n - R _W (counts	P _r experi- montal	n tuco- retical
	(in.)	Coins & G	rimite)	minute)	der de rechande de el der springelige	migger with the representation
3 1.5 6 4.5	0.025 0.025 0.064 0.126	According to the second	4752 ± 31 4823 ± 32 4353 ± 32 4778 ± 32 4375 ± 32	3970 ± 51 1011 ± 52 1071 ± 52 1016 ± 52 1093 ± 52	1.010 ± 0.010 1.025 ± 0.010 1.012 ± 0.018 1.031 ± 0.010	1.010 1.005 1.007 1.021
8 non 3 1.5 6	0.136 0.025 0.025 0.025	46666	1051 ± 32 2507 ± 17 2605 ± 17 2605 ± 17 2610 ± 17	4069 ± 52 1805 ± 44 1903 ± 14 1823 ± 14 1823 ± 14	1.025 ± 0.010 1.055 ± 0.036 1.010 ± 0.035 1.013 ± 0.035	1.007 1.023 1.010 1.006
6 8 4.5	0.004 0.064 0.126 0.126	6 6	2650 ±17 2577 ±17 2731 ±17 2643 ±17	1965 ± 14 1915 ± 14: 1910 ± 14: 1001 ± 14:	1.035 ± 0.035 1.006 ± 0.035 1.000 ± 0.036 1.031 ± 0.035	1.005 1.000 1.052 1.016

It was assured that this value of $R_{\rm g}$ remained constant with or without a citie ric 1 shell estable around the source and detector. It as a ray counting rater consected for $R_{\rm g}$ are listed in Table 4. The countilly determined total case are scattering rates are also listed. These ratios were calculated by Cividing the corrected for respectively rate with a cylindrical soll in continuous to the countries rate then as well was in scatter. The throughtest which of $R_{\rm g}$, calculated from a without (2h), and it and it we last

de . . , = , 4 . ___,/5 (-,0 ~ -- 2 3 2 4 d -6 11 11 4 -- 1 -. + . 9 2 * 4 ÷ ____

Annual of the second se

c lum of Table h.

An exceination of the experi much values of Ty shows that in certain and, they tend to expert the theoretical values are too broad to the any positive comparison between them and the theoretical values. For instance, with the cylindrical soll of 3 inches ratios and 0.025 inch shell their and uith h, equal to 6 inches, the percentage variation between the theoretical and the experis mich value as found from the equation,

is 3.12 ±3.52 per cent.

As in the entricanal results for neutron scattering, the p edominant contribution to the large deviations was the statistical variation in the calculated counting rate due to the air and the room scattering. This was reduced to the lowest possible value with the ec for nt and lable, but as is evident it was not reduced enough.

C. Grand Mecassion

It is believed that an a perimental procedure which will give useful results can be devised for measuring the radiation scale red by all rimm alloy cylindrical scales.

.00

.

endciency for counting fact reserves or a strong resource or a commission of these two world increase the probability of securing useful results. For an are counting, the taking of loner counts run is rowed results. Source, it is still a probability that the scattering caused by the air will do room build be the predominating factor in the statistical sourcey. If this is found to be true, another notice of experimental coursely. If this is found to be true, another notice of experimental coursely. If this is found to be true,

name room, the scattering caused by the sir and the room is mainly the to the latter. The , we be ical conclusion in to eliminate the room. his can be done by any ading the source, detector, and cylindrical shell from, say, a guide mire of a radio tower or some other shillar structure as was done by Glasgow (1). If the cap rimental system is some distance above the ground and for enough away from the tower or other magnetime, the system is essentially in an infinite air mains and the only exercised scatter would be from the air.

As a further relief no, the equations developed in this investigation for radiation scattering could be modified to include the scattering caused by the air. Chagos (1) gave an equation for set oring of newtrens in an include air medium and there that Colon (5) presented as a matter for the ray scattering by an infinite medium.

which had been presented as the present of the party of t which was I be to be a proper of the later and the passes of the later and the later a and and problems of a United Street Contract of the Contract o and the latter of the latter o . the second second live and the second water to the second to the sec SQ Indiana page 111 man and a man an

VIII. C KILIS O L

The experimental re ults, without tending to support the theoretical arms ray scatterin calculations, did not prove or disprove the analytical investigation results.

A one elaborate cop ris dal system and procedure and a nore efficient fast neutron det eter or a suremer source or both would probably be needed to secure of all sports atal results.

The scattering of neutrons and plant rays by the air and the room was the proceeding the large statistical deviations in the corrected counting rates. These statistical deviations were the jor cause of the peer results, although the low neutron counting rates were a contributing factor.

• . Company and a second se the second particle was to be a second to the second to th

VIII. LIL D'U. C'IM

- l. Clasjon, D. C. Meutron scattering from the walls and air of a laborator. Charles and air of a Control Walls and Service Products Control W-32086. June 9, 1954.
- 2. Pleset, 7. S. Scattering of government and neutrons. Douglas Aircraft Company, Project of Resport NAD-196. April 29, 1947. (Original not available or residuation; abstracted in Auctor Science Abstracts. 1: 522. 1948.)
- 3. Placet, 1. S. and others. iffect of surce and shadow shield geometry on the scattering of and rays. Douglas Aircraft Cornery, Project and coert AB-236. February 26, 1041. (Original not available for a function; abstracted in Ruchear Science Abstracts. 1: 630. 1048.)
- 4. Hine, Gereld J. and FeCall, Michard C. Germa-ra backscattering, Mucheonic . 12: 27-30. April, 1954.
- 5. Pleaset, M. S. and Cohen, S. T. Scattering and absorption of game-rays. Journal of Applied Physics. 22: 350-357. 1951.
- 6. Also aluminum and its alloys. Pittsburg, Pa., Aluminum Company of America. 1967.
- 7. Classtone, Squel and Edland, Hilton C. The elements of nuclear reactor theory. New York, D. Van hostrand Company, Inc. 1952.
- 8. Mansa, Gerald J. Garra dose rete from a Po-De source. Mucleanies. 12: 62. February, 1984.
- 9. Illiot, J. O. and others. In rg: spectrum of neutrons from Pole. Physical Leview. 93: 134-1349. 1954.

.000

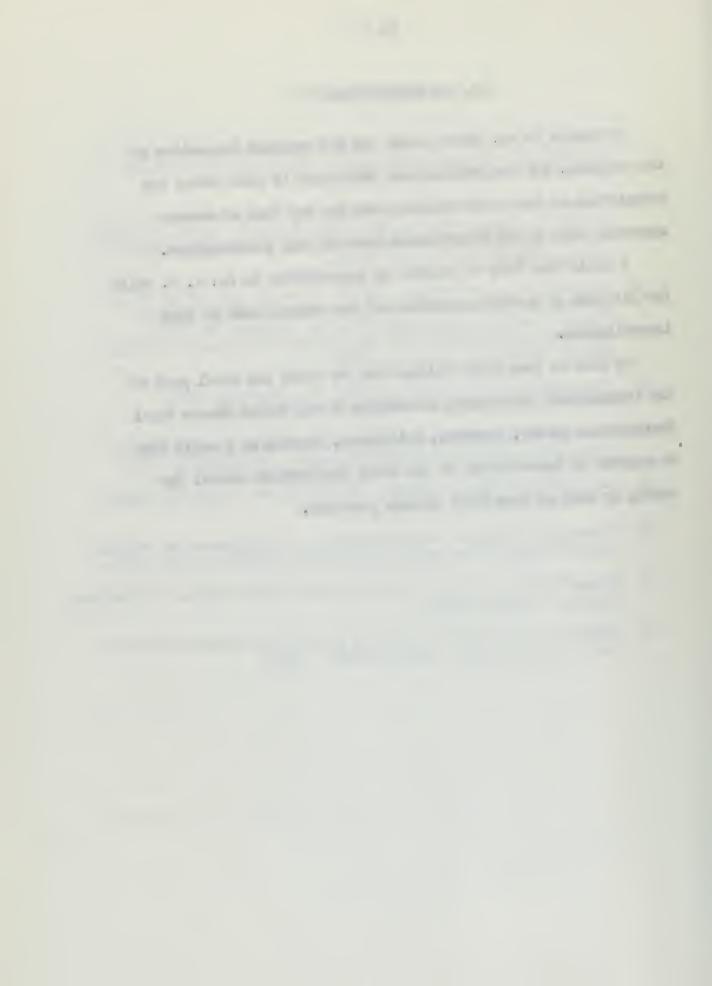
A TAX TAX DOS NAMES AND ADDRESS OF TAX ADDRESS OF T • A TO MITTER A TO THE REAL PROPERTY. £ 7 PRODUCE OF THE PRODUC THE RESERVE OF THE PARTY OF THE the second secon × - 11

IX. ACLEVITABLE THS

My thanks to Dr. Glenn Murphy for his original suggestion of this problem, for the guidance and help which he gave during our association at Towa State College, and for the loan of certain apparatus used in the experimental part of this investigation.

I would also like to express my appreciation to Dr. A. F. Voict for his lean of certain apparatus and the sources used in this investigation.

My work at Iowa State College was the third and final year of the Aeronautical Engineering Surriculum of the United States Haval Postgraduate School, Monterey, California, therefore, I would like to express my appreciation to the Naval Postgraduate School for making my work at Iowa State College possible.



X. AND MININ

A. Sample Analytical Computations

The average values of the solid eagle a subtended by the detector were calculated by using Equations (11), (12), and (13).

accimed to hear these A's were then served using Equation (13). For this particular cylindrical shell and detector, \overline{a} was found to be 0.367 storadians. This value is plotted on the upper curve of Figure 2 at r/h_h equal 0.1875.

The factor II which is plotted in Figure 3 was calculated using the equation

and the same of th 100 - The second secon ----

$$II = \ln \left[\left(\frac{1 - \sin \beta_b}{\cos \beta_b} \right) \left(\frac{\cos \beta_f}{1 - \sin \beta_f} \right) \right]$$

For θ equal -30 degrees and θ_{g} equal 70 degrees, substitution gave H equal 2.205.

The theoretical values of P., the total neutron scat aring ratio, are calculated using Equation (10). For this sample corputation a value of) inches for he end the cylinarical shell with 6 inches radius, 0.064 inch shell thickness and 16 i.ches neight was selected. The value of a for this cometry and the neutron detector used was taken from Figure 2. This value is 0.159 storadiens. The backward angle $oldsymbol{eta}_{s}$ for this peopetry is -39.8 degrees and the forward angle $eta_{_{\mathcal{S}}}$ is 61.4 degrees, thus the value of H as fiven in Figure 3 is 2.12. The mean free path for scattering, & was assumed to be constant at the thermal value throughout the energy spectra of neutrons can ted by this source. For the cladding wich is 5 per cent of the total thickness of the sheet, λ_s is 11.76 cm. and for the 24ST aluminum λ_s is 10.6 cm. Thus, $\lambda_{\rm s}$ for the Alched 2hBT is 0.05 times 11.76 cm. plus 0.95 times 10.60 cm. which is 10.66 cm. The detector angle eta_d for this detector and geometry is 11.75 degrees. Su stituting these values into Equation (18) gave R equal 1.034.

Equation (2h) was used to calculate the theoretical values of R

the same of the sa

THE RESIDENCE OF THE PERSON NAMED IN COLUMN 2 IN COLUM

The second secon

e e

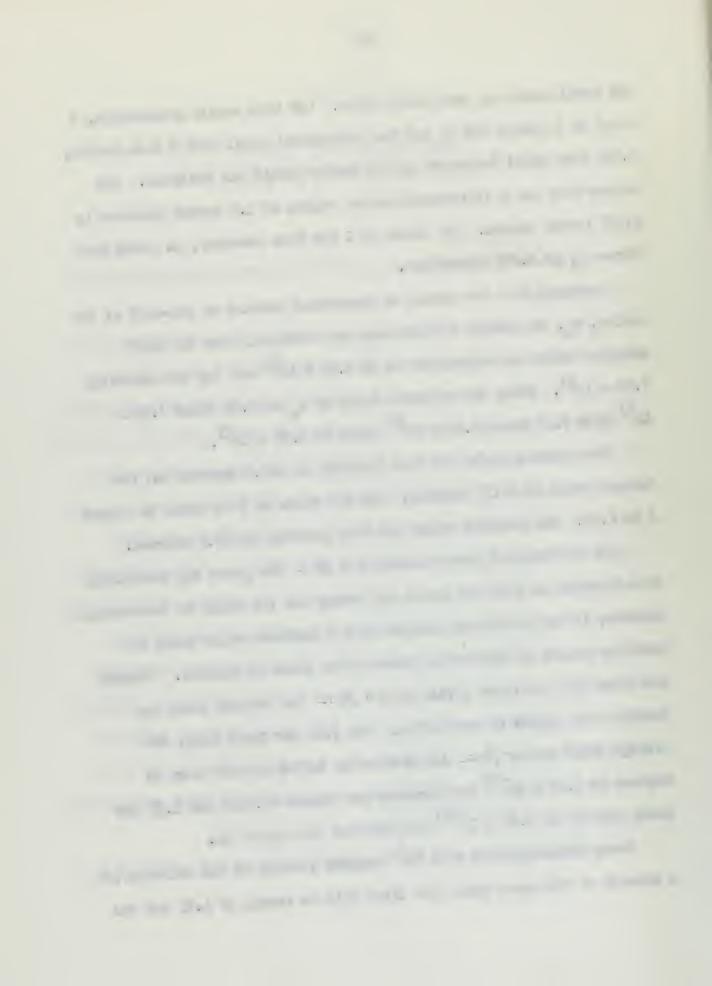
the total james ray scattering ratio. For this scaple calculation, a value of h inches for h_5 and the cylindrical shell with 6 inch radius, 0.06h inch shell thickness and 16 inches height was selected. The Ceiger tube has a cylindrical active volume of 1.5 inches diameter by 2.375 inches length. The value of $\bar{\lambda}$ for this geometry, as taken from Figure 2, is 0.952 storadians.

Assuming that the amount of impurities present is one-half of the ranks, n_e , the number of electrons per cubic cm., for the 2457 aluminum alloy was calculated to be 8.02 x 10^{23} and for the cladking, 7.93 x 10^{23} . Thus, the weighted value of n_e is 0.05 times 7.93 x 10^{23} plus 0.95 times 8.02 x 10^{23} which is 8.02 x 10^{23} .

The backward angle for this geometry is -50.0 degrees and the formula angle is 46.75 degrees, thus the value of H as given in Figure 3 is 2.17. The detector angle for this geometry is 10.6 degrees.

The differential cross section d σ /d Λ for game may scattering is a function of both the semi-ray energy and the angle of scattering. However, it was previously assumed that a constant value could be used for angles of scattering greater than about 70 degrees. Pleaset and Cohen (5) presented a plot of d σ /d Λ for various same ray energies and angles of scattering. For 1.02 Nev game rays, the average value of d σ /d Λ for scattering angles greater than 70 degrees is 0.89 x 10 per electron per square cm. and for 1.53 Nev game rays it is 0.64 x 10 per electron per square cm.

e caseace of two perma rays, the first with an energy of 1.17 New and



the second with an energy of 1.33 lev. It using straight like interpolation between the two values of d σ /d κ given above, d σ /d κ for the 1.17 Nov garma rays was found to be 3.02 x 10 $^{-26}$ per electron per square cm. and for the 1.33 lev garma rays it was evaluated as 0.74 x 10 $^{-26}$ per electron or a square cm. Since the number of κ a rays is said by the course are equal for each of the two energies, the final value of d σ /d κ was sound by multiplying each of the two values of d σ /d κ by 0.5 and adding. Thus d σ /d κ used in the equation for R is 0.75 x 10 per electron per source cm.

for L. .





thesN47
Similitude considerations in neutron and
3 2768 001 89957 8
DUDLEY KNOX LIBRARY